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# A-level MATHEMATICS

## Paper 2

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Exam Date

Morning

Time allowed: 2 hours

### Materials

For this paper you must have:

- The AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

### Instructions

- Use black ink or black ball-point pen. Pencil should be used for drawing.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

### Advice

Unless stated otherwise, you may quote formulae, without proof, from the booklet. You do not necessarily need to use all the space provided.

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**Section A**

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Answer **all** questions in the spaces provided.

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- 1** State the values of  $|x|$  for which the binomial expansion of  $(3 + 2x)^{-4}$  is valid.

Circle your answer.

**[1 mark]**

$|x| < \frac{2}{3}$

$|x| < 1$

$|x| < \frac{3}{2}$

$|x| < 3$

- 2** A zoologist is investigating the growth of a population of red squirrels in a forest.

She uses the equation  $N = \frac{200}{1 + 9e^{-\frac{t}{5}}}$  as a model to predict the number of squirrels,

$N$ , in the population  $t$  weeks after the start of the investigation.

What is the size of the squirrel population at the start of the investigation?

Circle your answer.

**[1 mark]**

5

20

40

200

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**3** A curve is defined by the parametric equations

$$x = t^3 + 2, \quad y = t^2 - 1$$

**3 (a)** Find the gradient of the curve at the point where  $t = -2$

**[4 marks]**

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**3 (b)** Find a Cartesian equation of the curve.

**[2 marks]**

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4 The equation  $x^3 - 3x + 1 = 0$  has three real roots.

4 (a) Show that one of the roots lies between  $-2$  and  $-1$

[2 marks]

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4 (b) Taking  $x_1 = -2$  as the first approximation to one of the roots, use the Newton-Raphson method to find  $x_2$ , the second approximation.

[3 marks]

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- 4 (c)** Explain why the Newton-Raphson method fails in the case when the first approximation is  $x_1 = -1$

**[1 mark]**

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**Turn over for the next question**



**5 (b)** Hence or otherwise find the least value and greatest value of

$$4 + (3\cos\theta + 3\sin\theta)^2$$

Fully justify your answer.

**[3 marks]**

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**Turn over for the next question**

**6** A curve  $C$ , has equation  $y = x^2 - 4x + k$ , where  $k$  is a constant.

It crosses the  $x$ -axis at the points  $(2 + \sqrt{5}, 0)$  and  $(2 - \sqrt{5}, 0)$

**6 (a)** Find the value of  $k$ .

**[2 marks]**

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**6 (b)** Sketch the curve  $C$ , labelling the exact values of all intersections with the axes.

**[3 marks]**

**Turn over for the next question**

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**Turn over ▶**

- 7 A student notices that when he adds two consecutive odd numbers together the answer always seems to be the difference between two square numbers.

He claims that this will always be true.

He attempts to prove his claim as follows:

**Step 1:** Check first few cases

$$3 + 5 = 8 \text{ and } 8 = 3^2 - 1^2$$

$$5 + 7 = 12 \text{ and } 12 = 4^2 - 2^2$$

$$7 + 9 = 16 \text{ and } 16 = 5^2 - 3^2$$

**Step 2:** Use pattern to predict and check a large example

$$101 + 103 = 204$$

subtract 1 and divide by 2 for the first number

Add 1 and divide by two for the second number

$$52^2 - 50^2 = 204 \text{ it works!}$$

**Step 3:** Conclusion

The first few cases work and there is a pattern, which can be used to predict larger numbers.

Therefore, it must be true for all consecutive odd numbers.

- 7 (a) Explain what is wrong with the student's "proof".

[1 mark]

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**7 (b)** Prove that the student's claim is correct.

**[3 marks]**

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**Turn over for the next question**



8 (b) Show that the  $x$ -coordinates of the points of inflection of the curve satisfy the equation

$$\cot 3x = \frac{9x^2 - 10}{6x}$$

**[4 marks]**

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- 9 (b)** Prove that there is no possible value of  $q$  for which  $3e^{-q}$ , 5,  $3e^q$  are consecutive terms of a geometric sequence.

**[4 marks]**

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**END OF SECTION A**  
**TURN OVER FOR SECTION B**

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**Section B**

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Answer **all** questions in the spaces provided.

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**10** A single force of magnitude 4 newtons acts on a particle of mass 50 grams.

Find the magnitude of the acceleration of the particle.

Circle your answer.

**[1 mark]**

$12.5 \text{ m s}^{-2}$

$0.08 \text{ m s}^{-2}$

$0.0125 \text{ m s}^{-2}$

$80 \text{ m s}^{-2}$ 

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11 A uniform rod,  $AB$ , has length 3 metres and mass 24 kg.

A particle of mass  $M$  kg is attached to the rod at  $A$ .

The rod is balanced in equilibrium on a support at  $C$ , which is 0.8 metres from  $A$ .



Find the value of  $M$ .

[2 marks]

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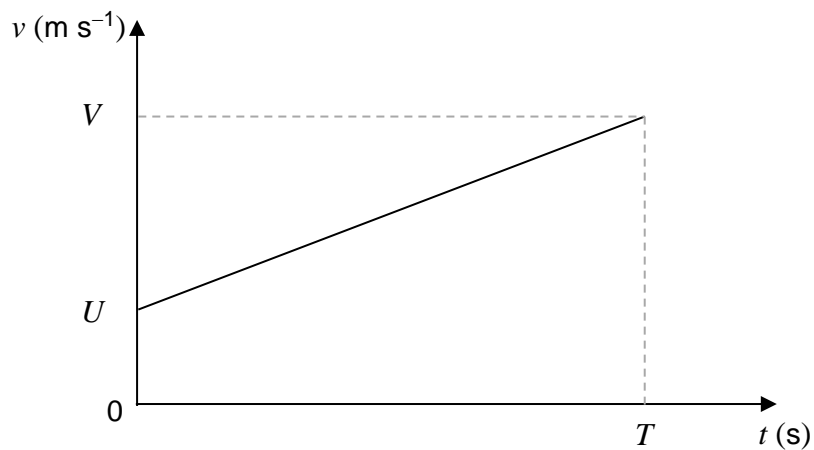
Turn over for the next question

12 A particle moves on a straight line with a constant acceleration,  $a \text{ m s}^{-2}$ .

The initial velocity of the particle is  $U \text{ m s}^{-1}$ .

After  $T$  seconds the particle has velocity  $V \text{ m s}^{-1}$ .

This information is shown on the velocity-time graph.



The displacement,  $S$  metres, of the particle from its initial position at time  $T$  seconds is given by the formula

$$S = \frac{1}{2}(U + V)T$$

12 (a) By considering the gradient of the graph, or otherwise, write down a formula for  $a$  in terms of  $U$ ,  $V$  and  $T$ .

[1 mark]

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**12 (b)** Hence show that  $V^2 = U^2 + 2aS$

**[3 marks]**

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**Turn over for the next question**

- 13** The three forces  $\mathbf{F}_1$ ,  $\mathbf{F}_2$  and  $\mathbf{F}_3$  are acting on a particle.

$$\mathbf{F}_1 = (25\mathbf{i} + 12\mathbf{j}) \text{ N}$$

$$\mathbf{F}_2 = (-7\mathbf{i} + 5\mathbf{j}) \text{ N}$$

$$\mathbf{F}_3 = (15\mathbf{i} - 28\mathbf{j}) \text{ N}$$

The unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are horizontal and vertical respectively.

The resultant of these three forces is  $\mathbf{F}$  newtons.

- 13 (a) (i)** Find the magnitude of  $\mathbf{F}$ , giving your answer to three significant figures.

**[2 marks]**

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- 13 (a) (ii)** Find the acute angle that  $\mathbf{F}$  makes with the horizontal, giving your answer to the nearest  $0.1^\circ$

[2 marks]

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- 13 (b)** The fourth force,  $\mathbf{F}_4$ , is applied to the particle so that the four forces are in equilibrium.  
Find  $\mathbf{F}_4$ , giving your answer in terms of  $\mathbf{i}$  and  $\mathbf{j}$ .

[1 mark]

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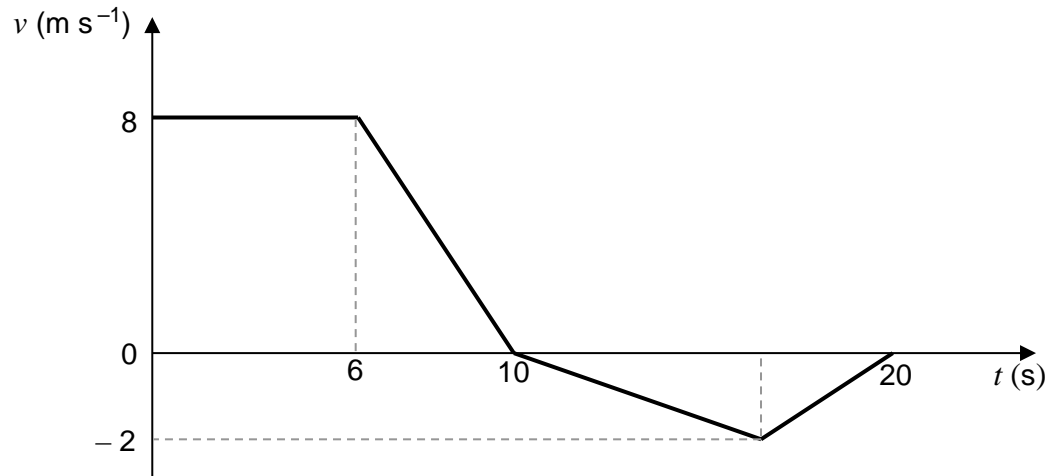
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Turn over for the next question

- 14 The graph below models the velocity of a small train as it moves on a straight track for 20 seconds.

The front of the train is at the point  $A$  when  $t = 0$

The mass of the train is 800kg.



- 14 (a) Find the total distance travelled in the 20 seconds.

[3 marks]

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**14 (b)** Find the distance of the front of the train from the point *A* at the end of the 20 seconds. **[1 mark]**

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**14 (c)** Find the maximum magnitude of the resultant force acting on the train. **[2 marks]**

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**14 (d)** Explain why, in reality, the graph may not be an accurate model of the motion of the train. **[1 mark]**

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- 15 (b)** The parachutist opens her parachute when she has travelled 100 metres horizontally.  
Find the vertical displacement of the parachutist from the origin when she opens her parachute.

**[4 marks]**

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- 15 (c)** Carefully, explaining the steps that you take, deduce the value of  $g$  used in the formulation of this model.

**[3 marks]**

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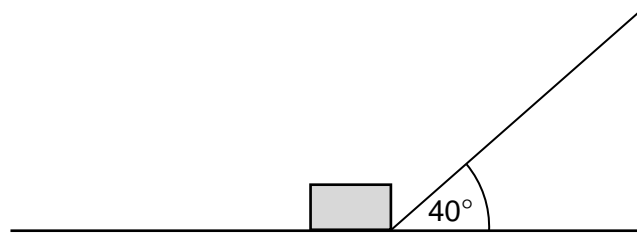
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16 In this question use  $g = 9.8 \text{ m s}^{-2}$ .

The diagram shows a box, of mass  $8.0 \text{ kg}$ , being pulled by a string so that the box moves at a constant speed along a rough horizontal wooden board.

The string is at an angle of  $40^\circ$  to the horizontal.

The tension in the string is  $50 \text{ newtons}$ .



The coefficient of friction between the box and the board is  $\mu$

Model the box as a particle.

16 (a) Show that  $\mu = 0.83$

[4 marks]

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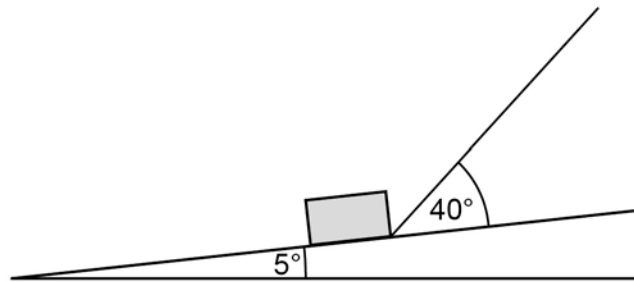
**Question 16 continues on the next page**

**16 (b)** One end of the board is lifted up so that the board is now inclined at an angle of  $5^\circ$  to the horizontal.

The box is pulled up the inclined board.

The string remains at an angle of  $40^\circ$  to the board.

The tension in the string is increased so that the box accelerates up the board at  $3 \text{ m s}^{-2}$



**16 (b) (i)** Draw a diagram to show the forces acting on the box as it moves.

[1 mark]



**17** In this question use  $g = 9.81 \text{ m s}^{-2}$ .

A ball is projected from the origin. After 2.5 seconds, the ball lands at the point with position vector  $(40\mathbf{i} - 10\mathbf{j})$  metres.

The unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are horizontal and vertical respectively.

Assume that there are no resistance forces acting on the ball.

**17 (a)** Find the speed of the ball when it is at a height of 3 metres above its initial position.

**[6 marks]**

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**17 (b)** State the speed of the ball when it is at its maximum height.

**[1 mark]**

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**17 (c)** Explain why the answer you found in part **(b)** may not be the actual speed of the ball when it is at its maximum height.

**[1 mark]**

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**END OF QUESTIONS**

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